



Maths Studies Mini Topic Exams

# Mathematical Models

Recommended time: 40 minutes

### Question 1

[Maximum mark: 6]



A structural column of a building is in the shape of a cylinder with radius  $r$  m and height  $h$  m. The curved surface area of the column is  $5 \text{ m}^2$ .

- (a) Write down an equation in terms of  $r$  and  $h$  to describe this information. [2]
- (b) The height  $h$  of the column is equal to its diameter. Calculate the value of  $r$ . [4]

## Question 2

[Maximum mark: 6]



Atmospheric pressure,  $P$ , in kPa, decreases exponentially with increasing height above sea level,  $h$ . The atmospheric pressure can be modelled by the function

$$P(h) = 101 \times \left(\frac{25}{22}\right)^{-h},$$


where  $h$  is the height above sea level in kilometres.

- (a) Write down the exact atmospheric pressure at sea level, in kPa. [1]

Mount Kosciuszko is the highest mountain in Australia with a height of 2228 metres above sea level at the top.

- (b) Calculate the atmospheric pressure at the top of the Mount Kosciuszko. [2]  
(c) Calculate the height where the atmospheric pressure is equal to 10 kPa. [3]

### Question 3

[Maximum mark: 13] 

A cannon-ball is fired from the top of a tower. The height,  $h$ , in metres, of the cannon-ball above the ground is modelled by the function:

$$h(t) = -2t^2 + 20t + 8, t \geq 0,$$

where  $t$  is the time, in seconds, since the moment the cannon-ball was fired.

(a) Write down the height of the tower. [1]

(b) Calculate the height of the cannon-ball 5 seconds after it was fired. [2]

The cannon-ball hits its target on the ground  $n$  seconds after it was fired.

(c) Find the value of  $n$ . [2]

(d) Find  $h'(t)$ . [2]

(e) Calculate the maximum height reached by the cannon-ball, and write down the corresponding time  $t$ . [3]

(f) Determine the total time the cannon-ball was above the height of the tower. [3]